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# **DIGEST BOOK**

**FEBRUARY 13 – 15, 2013**  
**SHARIF UNIVERSITY OF TECHNOLOGY**  
**TEHRAN, IRAN**

## Wheeled Mobile Robots II

Chairs: Hamid D. Taghirad, K. N. Toosi Univ. of Technology

Ali Khaki-Sedigh, K. N. Toosi Univ. of Technology

16:40 – 17:10 1162

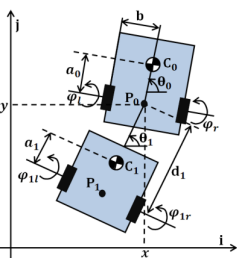
WeC2.1

### Modified Transpose Jacobian for Control of a Tractor-Trailer Wheeled Robot

Ali Keymasi Khalaji and S. Ali A. Moosavian

Dept. of Mechanical Eng., K.N.Toosi Univ. of Tech., Tehran Iran

- Kinematic equations of a tractor-trailer wheeled mobile robot are obtained.
- Reference trajectories for tracking problem are produced.
- A non-model-based control law is elaborated based on Modified Transpose Jacobian (MTJ) method for trajectory tracking of the Tractor-trailer wheeled mobile robot.
- Effectiveness of the proposed control law is verified in using Experimental studies.



17:10 – 17:30 1228

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### A Virtual Structure-based Approach to Formation Control of Cooperative Wheeled Mobile Robots

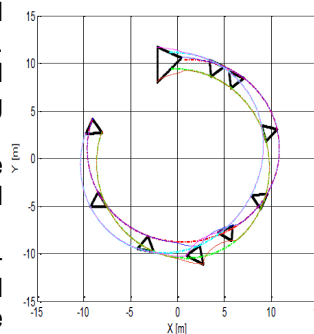
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- Controlling a group of mobile robots to provide a desired formation under perturbation.
- A virtual structure control strategy with mutual coupling between robots is proposed.
- The formation as a whole should follow a predefined trajectory.
- Each robot mediates between keeping formation and ensuring the tracking of the desired trajectory.



Robots formation under perturbations

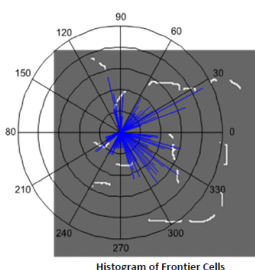
17:30 – 17:50 1297

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### سامانه تولید نقشه معنایی محیط توسط ربات خودمختار با استفاده از اکتشاف مبتنی بر هیستوگرام

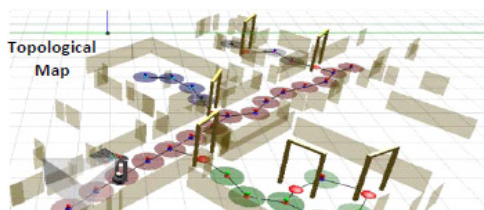
امیر مبرهنی، حمیدرضا تقی‌راد

دانشکده برق و کامپیوتر، دانشگاه صنعتی خواجه نصیرالدین طوسی، ایران



Histogram of Frontier Cells

- سامانه‌ای یکپارچه و هوشمند جهت تولید خودکار نقشه معنایی از یک محیط واقعی.
- تولید نقشه معنایی چند لایه با صحت ۹۰٪
- پیاده‌سازی حافظه کوتاه مدت در فرآیند مکان‌یابی معنایی
- شناسایی مناطق معنایی محیط بر اساس ویژگی‌های عمومی و محلی تصاویر دریافتی
- هدایت هدفمند ربات برای تولید نقشه معنایی توسط اکتشاف سریع و کامل محیط
- روشی کم‌پردازش و مبتنی بر هیستوگرام مناطق ناشناخته



17:50 – 18:10 1116

WeC2.4

### A New Method for Mobile Robot Navigation in Dynamic Environment: Escaping Algorithm

Farnaz Adib Yaghmaie, Amir Mobarhani, Hamid D. Taghirad

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- This paper addresses a new method for navigation in dynamic environment. The proposed method is based on forcefield method and it is supposed that the robot performs SLAM and autonomous navigation in dynamic environment without any predefined information about dynamic obstacles.
- The movement of dynamic obstacles is predicted by Kalman filter and is used for collision detection purpose. In the time of collision detection, a modifying force is added to repulsive and attractive forces corresponding to the static environment and leads robot to avoid collision.
- Moreover, a safe turning angle is defined to assure safe navigation of the robot. The performance of proposed method is verified through different simulation and experimental tests.
- The results show the proper performance of Escaping Algorithm in term of dynamic obstacle avoidance and it can be concluded that this method outperforms traditional methods in practice.

# A New Method for Mobile Robot Navigation in Dynamic Environment: Escaping Algorithm

Farnaz Adib Yaghmaie, Amir Mobarhany, and Hamid D. Taghirad

**Abstract**—In this paper, a new method for navigation in dynamic environment is suggested based on force field method. The robot performs SLAM and autonomous navigation in dynamic environment without any predefined information about dynamic obstacles. The movement of dynamic obstacles is predicted by Kalman filter and is used for collision detection purpose. In the time of collision detection, a modifying force is added to repulsive and attractive forces corresponding to the static environment and leads robot to avoid collision. Moreover, a safe turning angle is defined to assure safe navigation of the robot. The performance of proposed method is verified through different simulation and experimental tests. The results show the proper performance of Potential Ban in term of dynamic obstacle avoidance and it can be concluded that this method outperforms traditional methods in practice.

## I. INTRODUCTION

Path planning is needed for all mobile robots to perform a predefined task. Usually robots need a collision free path toward the target. It is important to note that the environment is unknown and as a result the robot plans a path while it is moving and gathering data. One of the most common methods for path planning is potential field. In this method, obstacles exert repulsive force to the robot while the target provides attractive force to it. The robot moves toward target avoiding obstacles based on the resultant of attractive and repulsive forces. This method is introduced by [1] and then improved for real time implementations [2]. Potential field is a popular method for mobile robot navigation due to its simplicity and implementation.

First, potential Field approach was suggested for navigation in static environment [3], [4], [5], [6]. However, the real world is not stationary, and the robot moves in dynamic environment and encounters dynamic obstacles like moving humans. Hence it should plan to reach the target without colliding with any static or dynamic objects. Researchers started to develop potential field methods for navigation in dynamic environment. In [7], the velocity of dynamic obstacles are included in the definition of potential function. The basic problem is that the collision depends on the velocity of both robot and obstacle; however, [7], considers only the speed of robot. In [8] relative positions and velocities of mobile robot with respect to obstacles are considered in definition of potential function. However, this method needs exact knowledge of velocity of dynamic objects, which is not available in practice. Potential function to reach a moving target is defined in [9], but the velocities of robot, obstacles and target are assumed to be known

In this paper, a different approach is suggested for velocity

planning of a mobile robot to navigate in dynamic environments based on potential field approach. The proposed method is called Escaping Algorithm (EA), and does not need any pre-knowledge information about dynamic obstacles. This method uses Kalman filter to predict the motion of dynamic objects and combines them with potential field approach to navigate safely in dynamic environment. EA has been simulated several times and implemented on a mobile robot platform. The reported results in this paper show the effectiveness of EA in term of dynamic obstacle avoidance and target tracking without need of expensive computations.

This paper is organized as follows: Section 2 provides environment representation and formulates the problem. The definitions of attractive and repulsive force in static environment are mentioned in this part. In section 3, escaping algorithm and its components are enlightened and the required steps to obtain repulsive force of dynamic obstacles are discussed. Simulation and experimental results of EA in dynamic environment are represented in section 4, and finally, concluding remarks are given.

## II. THE ENVIRONMENT MODELING AND PROBLEM FORMULATION

### A. The Environment Modeling

In this paper, the popular occupancy grid map is used for environment modeling [10]. The occupancy grid map uses a matrix to represent obstacles. Each entity in matrix is a symbol of one square part of environment and its quantity shows the confidence of the obstacle lying at this location. Greater value of certainty, greater possibility for existence of an obstacle in specific square. As a result, certainty values range from  $-\infty$  to  $+\infty$  in occupancy grid maps. The robot is equipped by one laser range finder and two encoders. Since laser is used to obtain information from environment, this map is suitably adapted to our system. In each range reading, the values of certainties are updated and used for navigation purposes.

### B. Problem Formulation

The motion planning problem of a mobile robot is to plan and control it such that it reaches the target while avoiding obstacles. In Force Field Method (FFM) the obstacles exert repulsive force to the robot while the target attract the robot to itself. The total force determines the direction of movement for the robot. The definitions of attractive and repulsive forces are not unique, and different definitions can be found in [11] and [9].

To use FFM for the mobile robot navigation, it is enough to suitably define the repulsive force of static objects, the attractive force of target and the repulsive force of dynamic objects and use their total direction for mobile robot steering. The last component will be explained in next section with more details.

#### 1) The Repulsive Force of Static Objects:

Since grid map is used for environment representation, the repulsive forces of static objects are defined for each occupied cell in grid map. To accomplish this task, it is needed to define a window on the robot coordinates and calculate the repulsive forces through it. This window is called active window and is used to avoid local obstacles while moving toward the target. For each cell in active window the repulsive force of static cell is calculated as follows.

$$f_r(i, j) = -\frac{F_{cr}C(i, j)}{d_{i,j}^2} \left[ \frac{x_{i,j} - x_r}{d_{i,j}} \hat{x} + \frac{y_{i,j} - y_r}{d_{i,j}} \hat{y} \right] \quad (1)$$

in which,  $F_{cr}$  is the repulsive force constant,  $C(i, j)$  denotes the certainty of cell(i,j),  $d_{i,j}$  denotes the distance between the robot and cell(i,j),  $(x_{i,j}, y_{i,j})$  is the position of cell(i,j), and  $(x_r, y_r)$  is the position of the robot. Total repulsive force is calculated by adding all repulsive forces in active window:

$$F_r = \sum_{i,j \in \text{win}} f_r(i, j) \quad (2)$$

#### 2) The Attractive Force of the Target:

The robot moves toward the target while avoiding obstacle. As a result, it is not important that whether the target is located in the active window or not, it always exerts its attractive force to the robot by the following relation:

$$F_a = F_{ca} \left[ \frac{x_t - x_r}{d_t} \hat{x} + \frac{y_t - y_r}{d_t} \hat{y} \right] \quad (3)$$

in which,  $F_{ca}$  denotes attractive force constant,  $(x_t, y_t)$  is the target position, and  $d_t$  denotes the distance between the robot and the target.

#### 3) Total Force:

Definition of repulsive force of dynamic objects denoted by  $F_m$  and required steps are explained in details in the next section.

The total force is determined as the sum of the repulsive and attractive forces. The total force in static environment is derived from following equation:

$$F_t = F_r + F_a \quad (4)$$

The above force is used for avoiding local static objects while moving toward the target. If a collision is predicted, the repulsive force of dynamic object is added to the total force and the resultant force is used for navigation.

$$F_f = F_t + F_m \quad (5)$$

The direction of  $F_f$  is used as steering rate command as follows. In static environment,  $F_m$  is equal to zero; in the

other words  $F_f$  and  $F_t$  are the same. Let  $\delta$  shows direction of  $F_f$ . If robot direction is denoted by  $\theta$ , angular velocity can be given by:

$$\omega = K_s(\delta - \theta) \quad (6)$$

in which,  $K_s$  is the steering constant whose dimension is  $(s^{-1})$ . This constant is set as the inverse of the sampling time.

### III. ESCAPING ALGORITHM: A STRATEGY FOR NAVIGATION IN DYNAMIC ENVIRONMENT

In static environment, the mobile robots can reach the target by using repulsive forces of static objects and attractive force of the target. However, it needs to perform four steps sequentially, to move in dynamic environment safely. These steps are as follows: moving objects detection, motion prediction, collision detection and velocity planning for obstacle avoidance. These sub programs are executed within the Simultaneous Localization And Mapping (SLAM) algorithm and use the grid map obtained from SLAM in their calculations. Each sub program is explained in following section with more details.

#### A. Moving Objects Detection

Moving object detection is one of the most important parts of planning in dynamic environment. The objective is to classify observations as static or dynamic. Researchers develops several methods for this classification. One common method is Expectation Maximization Algorithm (EMA) [12], [13]. EMA is a two steps maximization process which solves incomplete data optimization problem [14]. Another method is sample-based variant of probabilistic data association filter. This method filters dynamic observations like human and results robust scan matching [15]. Besides, non-probabilistic methods are also developed. For example, [16] suggested a simple rule for classification. This method is extended for grid map and is used for dynamic observation mapping in this paper.

In this paper a three-state map named dynamic map is generated and used for dynamic object detection. The dynamic map has similar structure to grid map and represents environment by set of cells. Each cell in this map can be labeled as free, occupied or unknown. A reading is associated to dynamic object if it locates in a free cell. The dynamic map is generated by following formula at each SLAM loop:

$$c_d(i, j) = \begin{cases} \text{free} & \text{if } c(i, j) < c_{min} \\ \text{occupied} & \text{if } c(i, j) > c_{max} \\ \text{unknown} & \text{otherwise} \end{cases} \quad (7)$$

In above,  $c_d(i, j)$  shows the cell  $(i, j)$  in dynamic map. The values of  $c_{min}$  and  $c_{max}$  are tuned practically. Using dynamic map, observations are divided to dynamic and static. Static observations are used in grid map, while dynamic observations are predicted and special strategy is used to avoid them. Please note that several sequential dynamic observations refer to of one moving objects because moving objects like human

Navigation in dynamic environment using potential field method is widely studied in literature. In this method, the target exerts attractive force to the robot, while static and dynamic objects apply repulsive forces. There are different definitions for the repulsive and attractive forces. For example in [9] a moving target is considered and the repulsive and attractive forces are derived by supposing full knowledge of the target and obstacle's positions and velocities. The final output of method suggested in [9] is a function of the target velocity and the relative positions between the obstacles, the target and the robot. Similarly, by considering full knowledge about moving objects and the target, in [8] relative distance and velocity between the robot and the obstacle are used in

repulsive force definition. The attractive force is defined based on relative distance and velocity between the robot and the target. One key problem of this method is that they need exact knowledge of position and velocity of dynamic obstacle and the target. However, this is an unrealistic assumption as none of them is known in practice.

In this paper Escaping Algorithm (EA) is suggest for obstacle avoidance. This algorithm is originated from a common behavior of human. A person usually intends to move in opposite direction in order to avoid colliding with a moving person. The same strategy can be used for mobile robot navigation. In our approach, the robot tries to moves in opposite direction if possibility of collision is detected. Consider Fig. 1. In this figure, obstacle direction in global frame is denoted by angle  $\alpha$ . The projection of this direction in robot frame is a suitable direction to align a new repulsive force. In order to perform that, the velocity of obstacle is expressed in the robot frame by the following rotation.

$$\begin{aligned} V_{obs}^r &= \begin{bmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} V_{obs} \cos(\alpha) \\ V_{obs} \sin(\alpha) \end{bmatrix} \\ &= \begin{bmatrix} V_{obs} \cos(\alpha - \theta) \\ V_{obs} \sin(\alpha - \theta) \end{bmatrix} \end{aligned} \quad (12)$$

In Fig. 1,  $F_t$  denotes the total force considering static environment. The obstacle velocity which is projected in the robot frame is used to define modifying force  $F_m$ . This new force has the same norm as  $F_t$  and its direction is opposite to the obstacle direction in  $x$ , and parallel to it in  $y$  direction. Any time that possibility of a collision is detected, the modifying force  $F_m$  is added to the total force and the final force  $F_f$ , is used for steering the robot toward the target.

To consider the safety of motion, consider Fig. 2. As it is mentioned before, it is supposed that the robot and the obstacle can be modeled by circles with radius  $R_{obs}$  and  $R_{rob}$  respectively. It is similar to consider the robot as a point and enlarge the radius of obstacle to  $R_{obs} + R_{rob}$ . As a result the minimum turning angle for the robot is  $\varphi$  to avoid collision. This angle is shown in Fig. 2 and may be derived by the following equation.

$$\varphi = \arcsin\left(\frac{R_{rob} + R_{obs}}{d}\right) \quad (13)$$

In the above equation,  $R_{rob}$  is a known parameter and can be measured before test.  $R_{obs}$  is calculated as it is explained in section 3-A. To assure safety, if the turning angle  $(\delta - \theta)$ , is less than  $\varphi$ , the the turning angle  $\varphi$  is considered for robot steering.

#### IV. RESULT

In this part the simulation and experimental results of using EA in dynamic environments are presented. It is important to note that navigation by using force field family suffers from trapping in local minima. This problem occurs when the robot

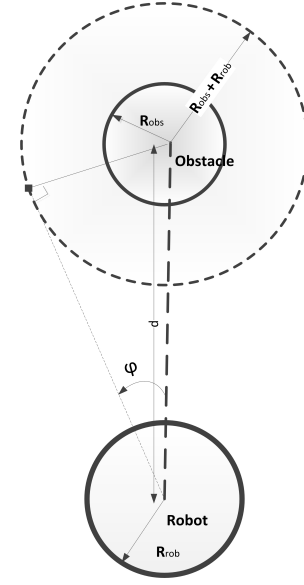


Fig. 2: Definition of safe turning angle

direction differs more than 90 degrees off target or  $F_f$  is equal to zero.

$$|\delta - \theta| > \frac{\pi}{2} \quad (14)$$

$$|F_f| = 0 \quad (15)$$

Researchers develop several recovery methods to encounter local minimum problem. For example recovery methods based on electromagnetic field and modification of repulsive potential functions are suggested in [17] and [8] respectively. One of the most popular recovery methods is Wall Following Method (WFM) which is suggested in [1]. In this context, WFM is used for mobile robot navigation to avoid trapping in local minima.

##### A. Simulation Result

In this section, simulation result of using EA in a dynamic environment is described. For simulation, seven dynamic objects are considered whose positions and motion directions

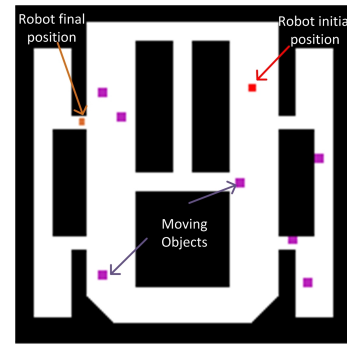


Fig. 3: The global map in which the robot reads observations

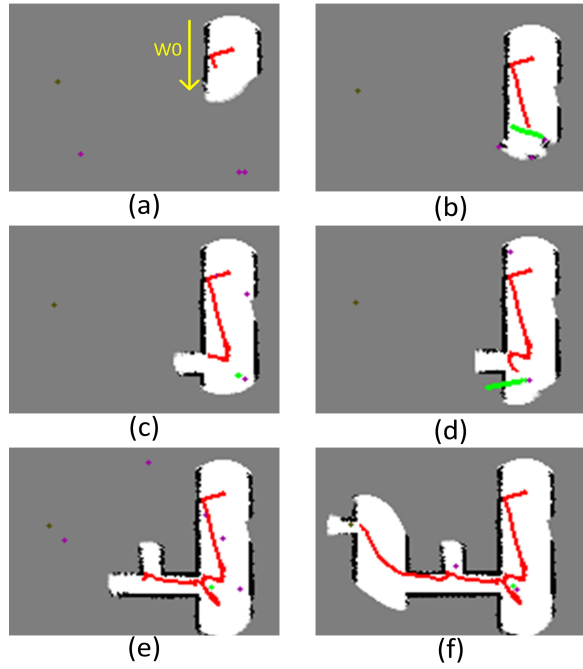


Fig. 4: Robot path in dynamic environment using EA

are randomly selected. The robot does not have any prior knowledge about moving objects and their paths are estimated by Kalman filter. The robot obtains its observation from global map shown in Fig. 3. In this figure, the start point, the target point and seven dynamic objects are shown. The robot navigates from the start point to the target point successfully, provided that it does not collide with static and dynamic objects.

It is possible that several collisions are detected at some occasions by collision detection algorithm. In these situations, only the nearest threat is considered and others are neglected. After eliminating the nearest danger, the next hazardous collision is considered. In Fig. 4 the performance of EA in dynamic environment is depicted. As it is seen in this figure, the robot starts moving to the target in (a). The wall  $w_0$  bans the robot path. As a result, the robot follows it. The robot faces a moving object in (b) and the modifying force is executed and causes the robot to move in opposite direction of the moving object. When the threat of collision is removed, the robot turns to the target in (c). However, appearance of another moving object causes the robot to turn off the target again to avoid it. This movement is depicted in (d). After using EA for dynamic obstacle avoidance, the robot turns to the target and moves toward it in (e). Finally, the robot reaches the target in (f).

Fig. 4 shows only one of several simulation tests. Due to the fact that moving objects are located and directed randomly, almost all scenarios have been tested on the robot. In all of them, the robot was successful in its mission to reach the target and does not collide with any object through its movement. These set of simulations provides us enough assurance to implement this algorithm on the following real time experiments.

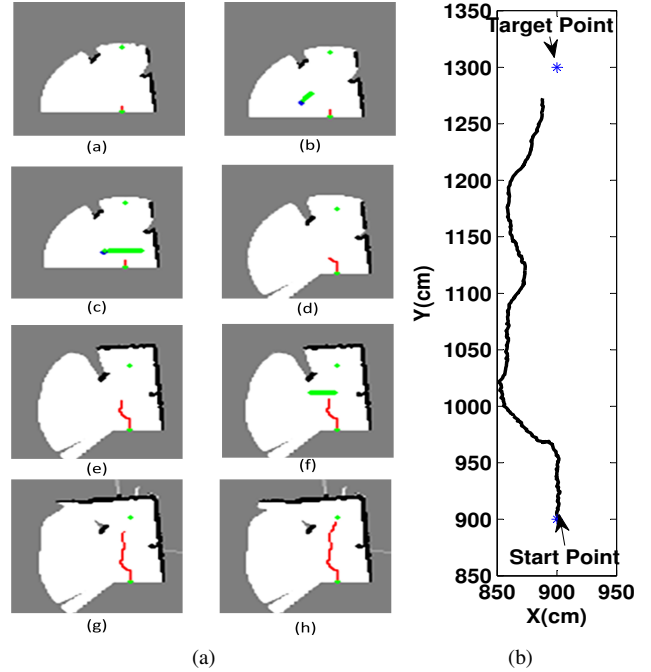


Fig. 5: EA experimental result in a more complex scenario

## B. Experimental Results

EA for navigation in dynamic environment is implemented on KNTU Mellon mobile robot. The mobile robot perceives environment through a laser range finder whose maximum range reading is 8 meter. The laser scan data is used for map building in a SLAM environment. The ego motion estimation is done by well-known ICP algorithm [18]. To achieve more accurate result in robot localization the odometry information by encoders mounted on two wheels, serves as the initial guess for ICP algorithm. A computer with core i5 processor is used for online execution of the algorithm. The algorithm contains a loop for simultaneous localization and mapping (SLAM) in addition to robot navigation routine.

For the control of Mellon mobile robot two commands are prompted, namely the velocity of the right and left wheels, denoted by  $\omega_r$ , and  $\omega_l$ , respectively. These velocities are easily obtained by linear transformation of linear and angular velocities as below:

$$\begin{bmatrix} \omega_r \\ \omega_l \end{bmatrix} = \frac{1}{r} \begin{bmatrix} 1 & \frac{b}{2} \\ 1 & -\frac{b}{2} \end{bmatrix} \begin{bmatrix} V \\ \omega \end{bmatrix} \quad (16)$$

where,  $r$  and  $b$  denote radii of wheel and wheel base, respectively. The angular velocity (6) is calculated by considering (5) in EA. Different methods are suggested by researchers [9], [2] for linear velocity definition. In this context, since fast performance of the mobile robot is desired, it is good that the mobile robot moves as fast as possible. However, it should start deceleration before an obstacle appears in its path in order to avoid collision. Hence, it is suitable that the mobile robot moves with its maximum linear velocity until it reaches



the region that should decelerate to stop completely near an obstacle. Hence,

$$V = \begin{cases} V_{max} & \text{if } d_{min} > d_{eff} \\ \frac{d_{min}}{d_{eff}} V_{max} & \text{otherwise} \end{cases} \quad (17)$$

In (17),  $d_{min}$  is the minimum range reading in range scanning and  $d_{eff}$  is the distance passed by the robot when it decelerates from maximum velocity to zero.

In what follows, experimental result of using EA in dynamic environment is given. In this experiment, the target is located in front of the robot with a relative distance of  $4m$ . While the robot tries to reach target with a distance less than  $30cm$ . In the terms of static environment, the robot goes straight to the target until it approaches static obstacle and tries to avoid it. However, the robot motion in dynamic environment is different. The dynamic scenario is run twenty two times and the result of one of them is shown in Fig. 5

To examine the effect of dynamic environment, two moving objects approach the robot from the left. The robot tries to find a collision free path for safe navigation. As indicated in Fig. 5 and in part (a), the robot starts moving toward the target, while in (b) a moving obstacle appears and in (c) a collision possibility is detected. In (d) the robot turns left to avoid collision and again in (e) it moves back toward the target. Moreover, in (f) another collision possibility is detected and the modifying force is added to the total force, and hence, the robot turns to the left to avoid collision in (g). Finally, in (h) it reaches the target. Robot path using EA in this experiment can be observed in more detail in Fig. 5b. From the promising results observed in the set of twenty two experiments, we may conclude that EA algorithm is suitable to be used in further development of autonomous robots.

## V. CONCLUSION

In this paper, Escaping Algorithm is suggested for navigation in dynamic environments. This method introduces modifying force in addition to attractive and repulsive forces in a force field environment. EA does not need exact information such as velocity and position of dynamic obstacles. These properties are estimated by Kalman filter and the obtained results are used in defining the modifying force. The basic idea of EA is obtained from a common behavior of human in obstacle avoidance and it is turning object from behind. The general performance of proposed method is checked through several simulation in  $U$  shape environment with a different number of dynamic obstacles. Furthermore, the experimental results show the effectiveness of proposed method in practical implementation. Finally, it can be concluded from these observations that this method is successful in term of dynamic obstacle avoidance.

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