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# DIGEST BOOK

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#### **Cable Robots**

#### Chairs: Moharram Habibnejad Korayem, Iran University of Science and Technology Amin Nikoobin, Tarbiat Modares University



#### 15:40 - 16:00 1183

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طراحی یک ربات چهار کابلی فضایی و تحلیل اثر شتاب مجری نهایی بر روی کشش کابل ها

امین نیکوبین'، محمود رسولی'، مجتبی ثقفی پور فرد'، اسماعیل زمانی ً

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- در این مقاله به طراحی یک ربات چهار کابلی فضایی و تحلیل اثر شتابهای کارتزین مجری نهایی ربات بر روی کشش کابلها پرداخته میشود. مجری نهایی این ربات دارای سه درجه آزادی انتقالی است که حرکت آن توسط چهار کابل کنترل میشود.
- رباتهای کابلی نوعی از رباتهای موازی هستند که نکته مهم در رابطه با آنها در کشش بودن کابلها میباشد.بدین منظور بدست آوردن شتابهای مجری نهایی که شرط در کشش بودن کابلها را برآورده کنند، مهم میباشد.
  - با استخراج معادلات دینامیکی
     مجری نهایی و ساده سازی آنها،
     ارتباط کشش کابلها و شتابهای
     با مساوی صفر قرار دادن روابط
     کشش کابلها، مرز شتابهای
     قابل قبول برای برقراری شرط در
     کشش بودن کابلها، بدست می-



برای برقراری شرط در کشش بودن کابلها، شتابهای مجری نهایی باید بزرگتر و مساوی این شتابها در نقاط انتخابی در صفحه z-x باشند.

### Kinematic Performance Indices Analyzed on Four Planar Cable Robots via Interval Analysis

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 In this paper, four designs of planar cablerobots are studied by following indices, via interval analysis.

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- Feasible kinematic sensitivity and worst kinematic sensitivity indices have been used to determine the efficiency of the robot workspace.
- The fabrication feasibility, mechanical interference and the moving platform volume are considered as other design indices.
- By considering results obtained from the above analysis, an acceptable design was selected for fabrication.



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U-inverted U design, Acceptable mechanism forfabrication

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## A Positive Tensions PID Controller for a Planar Cable Robot: An Experimental Study

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*Abstract*—In this paper design and control of planar cabledriven parallel robots are studied in an experimental prospective. Since in this class of manipulators, cable tensionability conditions must be met, feedback control of such robots becomes more challenging than for conventional robots. To meet these conditions, internal force control structure is introduced and used in addition to a PID control scheme to ensure that all cables remain in tension. A robust PID controller is proposed for partial knowledge of the robot, to keep the tracking errors bounded. Finally, the effectiveness of the proposed control algorithm is examined through experiments on K.N. Toosi planar cable–driven robot and it is shown that the proposed control structure is able to provide suitable performance in practice.

#### I. INTRODUCTION

Although the robots are extensively used in industries, their applications in long-reach robotics is limited and still is in infancy. Conventional robots with serial or parallel structure are impractical for such applications due to their limited workspace. for these reasons, cable-driven robots have received more attention in the past two decades. Cable-driven robots are a special class of parallel robots in which cables replace rigid links in the robot structure. In a cable-driven robot the end-effector is connected to the base by a number of active cables and by controlling the cables lengths, the pose of the end-effector is shifted toward the desired position and orientation. Cable-driven robots possess some useful properties such as large workspace capability, transportability and ease of assembly/disassembly, reconfigurability and economical structure and maintenance [1]. As a result, cable-driven robots are exceptionally suitable for many applications such as, handling of heavy materials [2], high speed manipulation [3], [4], cleanup of disaster areas [5], very large workspace applications [6], [7], and interaction in hazardous environment [8].

However, replacing rigid links by cables, introduces new challenges in the study of cable-driven robots which are quite different from that of conventional robots. Unlike the rigid links, cables can only apply tensile forces. Due to this physical limitation, well-known control theories can not be used directly for cable-driven robots and they must be modified such that they can provide positive tension for the cables. In comparison with the large amount of articles published on the control of conventional robots, relatively less has been published on the control of cable-driven robots. With assumption



Fig. 1. K.N. Toosi planar cable-driven robot.

of massless rigid string model for the cables, many of control schemes which have been used for conventional robots, may be adapted for cable robots. PD control in companion with gravity and internal forces in the cable-length coordinates [3], PD control with gravity in task space coordinates [9], and Inverse Dynamics Control (IDC) [9], [10], [11], are some control algorithms which are used in control of cable-driven robots.

The goal of this paper is to practically develop a control algorithm based on popular PID for position control of K.N. Toosi planar cable-driven robot (Fig. (1)) and investigate experimental performance of such a control structure. In order to ensure that all the cables are in tension for all maneuvers in their workspace, internal force structure control is used in addition to the proposed control law. Next, the implementation issues are discussed and finally, experimental results are given to show the effectiveness of the proposed control algorithm in practice.

#### **II. SYSTEM KINEMATICS AND DYNAMICS**

K.N. Toosi planar cable-driven robot consists of an endeffector that is connected by four cables to the base platform



Fig. 2. The schematics of K.N. Toosi planar cable-dricen robot.

as shown in Fig. (2). As it is shown in Fig. (2),  $A_i$  denote the fixed base points of the cables,  $B_i$  denote connection points of the cables on the end-effector,  $l_i$  denote the cable lengths, and  $\alpha_i$  denote the cable angles. The position of the end-effector center of mass P, is denoted by  $P = [x_P, y_P]$ , and the orientation of the manipulator end-effector is denoted by  $\phi$  with respect to the fixed coordinate frame. Hence, the manipulator posses three degrees of freedom  $x = [x_P, y_P, \phi]$ , with one degree of actuator redundancy.

#### A. Kinematics and Jacobian

For kinematic analysis, as it is shown in Fig. (3-a), a fixed frame O: xy is attached to the fixed base at point O, the center of the base point circle which passes through  $A_i$ . Moreover, another moving coordinate frame P: UV is located on the end-effector at its center of mass P. Assume that the point  $A_i$  lies at the radial distance of  $R_A$  from point O, and the point  $B_i$  lies at the radial distance of  $R_B$  from point P in the xy plane, when the manipulator is at central location. For inverse kinematics analysis, it is assumed that the position and orientation of the end-effector  $\boldsymbol{x} = [x_P, y_P, \phi]^T$  are given and the problem is to find the lengths variable of the manipulator  $\boldsymbol{L} = [l_1, l_2, l_3, l_4]^T$ . Let's define the instantaneous orientation angle of  $B_i^*s$ :

$$\phi_i = \phi + \theta_{B_i}$$

The loop closure equation for each cable (i = 1, 2, 3, 4), can be written as,

$$\overrightarrow{A_iP} = \overrightarrow{A_iB_i} + \overrightarrow{B_iP}$$

With some manipulation we can show that [12],

$$l_i^2 = (x_P - x_{A_i} + R_B \cos(\phi_i))^2 + (y_P - y_{A_i} + R_B \sin(\phi_i))^2$$

Furthermore, for the geometry of the manipulator as illus-



Fig. 3. (a) Kinematic configuration of mechanism (b): Vector definitions

trated in Fig. (3-b), the manipulator Jacobian matrix J is,

$$\boldsymbol{J} = \begin{bmatrix} S_{1x} & S_{1y} & E_{1x}S_{1y} - E_{1y}S_{1x} \\ S_{2x} & S_{2y} & E_{2x}S_{2y} - E_{2y}S_{2x} \\ S_{3x} & S_{3y} & E_{3x}S_{3y} - E_{3y}S_{3x} \\ S_{4x} & S_{4y} & E_{4x}S_{4y} - E_{4y}S_{4x} \end{bmatrix}$$
(1)

in which, the subscripts x, and y denote the corresponding components of the  $S_i$  and  $E_i$  vectors as shown in Fig. (3-b). Note that the Jacobian matrix J is a non-square  $4 \times 3$  matrix, since the manipulator is redundantly actuated.

#### B. Dynamic Model

Using massless rigid string model for the cable, the equations of motion for the planar manipulator can be written in the following form,

$$\boldsymbol{M}\ddot{\boldsymbol{x}} + \boldsymbol{G} = -\boldsymbol{J}^T\boldsymbol{\tau} \qquad \boldsymbol{\tau} \ge 0 \tag{2}$$

in which,  $\boldsymbol{x} = [x_P, y_P, \phi]$  and

$$M = \begin{bmatrix} m & 0 & 0 \\ 0 & m & 0 \\ 0 & 0 & I_z \end{bmatrix} \text{ and } G = \begin{bmatrix} 0 \\ mg \\ 0 \end{bmatrix}$$
(3)

where *m* is the mass and  $I_z$  is the moment of inertia of the end-effector about its center of mass. *J* denotes the Jacobian matrix of the manipulator, *g* is the gravitational acceleration and  $\tau$  denotes the vector of cables tension, i.e.,  $\tau = [\tau_1, \tau_2, \tau_3, \tau_4]$ . It should be noted that the above dynamic model is valid only for  $\tau \ge 0$  and as soon as the cables become slack, the structure of the robot collapses. All geometrical and mechanical parameters of the cable-driven robot are given in tables (I),(II).

#### III. PROPOSED CONTROLLER

As mentioned earlier, for the cable-driven robots control algorithms must be designed in such a way that all cables remain in tension during the motion of the end-effector in the whole workspace. In this section, we propose a practical control scheme based on popular PID. This algorithm uses internal force concept to ensure that all cables remain in tension. Furthermore, In design procedure of the controller it is assumed that all dynamic terms such as m and  $I_z$  are uncertain and we have only some information about their

 TABLE I

 POSITION OF THE CABLE ATTACHMENT POINTS

Fixed $A_i$ 's (m)	Moving $B_i$ 's (m)
$A_1$ (-1.12, +1.05)	$B_1$ (-0.155, 0)
$A_2$ (+1.12, +1.05)	$B_2$ (+0.155, 0)
$A_3$ (-1.12, -1.05)	$B_3$ (-0.155, 0)
A <sub>4</sub> (+1.12, -1.05)	$B_4$ (+0.155, 0)

bounds. Control gains of PID are tuned base on these bounds to satisfy some stability conditions. Recall dynamic model of the planar robot (2), in presence of uncertainties in all dynamical terms, it can be simply shown that if the end-effector mass is  $2.5 \ kg$  with a variation of  $0.5 \ kg$  payload then,

$$\underline{m} \leq \|\boldsymbol{M}(\boldsymbol{x})\| \leq \overline{m} , \ \overline{m} = 3 , \ \underline{m} = 0.08$$
$$\|\boldsymbol{G}(\boldsymbol{x})\| \leq 30$$

Now choose a controller for the system based on a PID by:

$$-\boldsymbol{J}^{T}\boldsymbol{\tau} = \boldsymbol{K}_{V}\dot{\boldsymbol{e}} + \boldsymbol{K}_{P}\boldsymbol{e} + \boldsymbol{K}_{I}\int_{0}^{t}\boldsymbol{e}(s)ds = \boldsymbol{K}\boldsymbol{y} \qquad (4)$$

in which,

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Since Jacobian matrix of the manipulator is a non-square  $4 \times 3$  matrix, (4) is an underdetermined system of equations and if  $J^T J$  is invertible it has many solutions. In this case, the general solution of (4) is,

$$\tau = \overline{\tau} + Q \tag{5}$$

Here,  $\overline{\tau}$  is the minimum solution of (4) derived by using the pseudo-inverse of  $J^T$  and is given by

$$\overline{\boldsymbol{\tau}} = -\boldsymbol{J}(\boldsymbol{J}^T\boldsymbol{J})^{-1} \left[ \boldsymbol{K}_V \dot{\boldsymbol{e}} + \boldsymbol{K}_P \boldsymbol{e} + \boldsymbol{K}_I \int_0^t \boldsymbol{e}(s) ds \right]$$
(6)

and, Q spans the null space of  $J^T$  which satisfies

$$\boldsymbol{J}^T \boldsymbol{Q} = \boldsymbol{0} \tag{7}$$

Furthermore, Q can be written in the following form,

$$\boldsymbol{Q} = \mathbb{N}(\boldsymbol{J}^T)c \tag{8}$$

where,  $\mathbb{N}(J^T)$  is the null space or kenel of matrix  $J^T$  which in this case is a  $4 \times 1$  vector and c is an arbitrary scalar. Q can be physically interpreted as *internal forces*. It means that this term does not contribute into the motion of the end-effector and only provides positive tension in the cables. In other words, input constraint  $\tau \geq 0$  is met using *internal forces* 

$$\overline{\tau} + Q \ge 0 \tag{9}$$

with this notation, the proposed control scheme can be implemented according to Fig. (4). In this paper we assume that

 TABLE II

 INERTIAL PARAMETER OF THE PLANAR CABLE-DRIVEN ROBOT

Parameter	Symbol	Value
End-effector mass	m	$2.5 \pm 0.5 \; Kg$
End-effector inertia	$I_z$	$0.1\pm0.02~Kg.m^2$
Gear ratio	Ν	50
Gravity Acceleration	g	9.8 m/ $s^2$
Drum radius	r	3.5 cm

at all times, positive internal forces can be produced such that the cables are in tension.

Implement the control law  $\tau$  in (2) to get the following relations for the closed loop system:

$$\dot{\boldsymbol{y}} = \boldsymbol{A}\boldsymbol{y} + \boldsymbol{B}\Delta\boldsymbol{A} \tag{10}$$

in which,

$$egin{aligned} & A = \left[ egin{array}{cccc} 0 & I_3 & 0 \ 0 & 0 & I_3 \ -M^{-1}K_I & -M^{-1}K_P & -M^{-1}K_V \end{array} 
ight] \ & B = \left[ egin{array}{cccc} 0 \ 0 \ M^{-1} \end{array} 
ight] \end{aligned}$$

and

$$\Delta \boldsymbol{A} = \boldsymbol{G}(\boldsymbol{x}) + \boldsymbol{M}\ddot{\boldsymbol{x}}_d \tag{12}$$

Khosravi and Taghirad in [13] have elaborated uniformly ultimately bounded (UUB) stability of a general cable-driven robot when control gains of PID are selected from a suitable feasible set. The proof of UUB stability is based on Lyapunov stability analysis for the uncertain system. For our implemented planar cable-driven robot, the controller gains are selected as  $K_P = 10000I_3$ ,  $K_V = 3000I_3$ ,  $K_I = 600I_3$ in the feasible stability region of the system considering the modeling uncertainty bounds. In this paper we leave the details of the proof, and verify the performance of the closed-loop system through experiments.

#### IV. EXPERIMENTAL SETUP

In this section some practical issues in design and implementation of K.N. Toosi planar cable-driven robot are investigated. It should be noted that mechanical design and the choice



Fig. 4. Internal force control structure.



Fig. 5. The system of cable winch

of electrical and mechanical components may significantly affect the overall performance of the manipulator. Thus, these subjects are of particular importance and should be consider in the design and implementation procedure of the manipulator.

#### A. Mechanical Structure

The base frame of the robot is implemented by extruded aluminum profile so that the vibrations are damped efficiently. These extruded profiles are common in many industrial assemblies. Moreover, four custom made systems of cable winches are placed on the base frame as cable actuators. The system of cable winch consists of an AC servo motor with a 1:50 gearbox which is attached to a drum. A special design is used in the cable winches by which the base attachment points of the robot are kept fixed. As it is shown in Fig. (5), this is accomplished by moving the drum along its axis with a pitch equal to the cable width. Furthermore, two touching ball bearings are used to guide the cable toward the end-effector.

Cable selection is another important issue in cable-driven robots. In this application, cables should be light and shall resist high loads and tensions. Furthermore, selected cable should be sufficiently stiff to have less elongation due to applied loads. For these reasons, polyethylene cable with tissue pattern  $1 \times 7$  has been selected for K.N. Toosi planar cable robot [14].

#### B. Control System Structure

The block diagram of the control system setup is shown in Fig. (6). The host computer serves as the user interface and enables the user to edit and modify models. Target is a real time processing unit which uses QNX operating system and performs real time execution of the model simulation and real time communication with I/Os. RT-LAB software works in conjunction with Matlab and Simulink to define models in real time environment. RT-LAB is designed to automate the execution of simulations for models made with Simulink, in a real time multiprocessing environment [15]. A number of PCI input/output boards were integrated with the RT-LAB and Simulink to create a real time control system.

To have a desirable performance in position and orientation tracking, servo drives should accurately provide the required tensions in the cables according to the proposed control algorithm. In other words, the servo drives shall be ideal force



Fig. 6. Control system setup

generators when seen by the proposed control algorithm. This is due to the fact, that in the procedure of control design it is assumed that the cables are rigid, but in practice this is not completely true. Based on this fact, cascade control scheme is implemented in the experiments to provide ideal force sources. The cascade control strategy uses two control loops, namely the outer loop and the inner loop as shown in Fig. (7). The main goal of the outer loop, which consists of the proposed PID control, is to control the position and orientation of the end-effector. Inputs of this loop are the position and orientation errors and its outputs are required tensions for the inner loop. In the inner loop, the desired tensions are compared to actual tensions measured by the load cells located near the end-effector attachment points. TLL500 from Transducer Techniques is used as load cell in our experiments. Moreover, internal force control structure is used to ensure us that all the cables remain in tension. The proposed controller is implemented using Matlab real-time workshop and RT-LAB software. The equations of forward kinematics is solved using CFSQP<sup>1</sup> routine [16] implemented as an sfunction in Simulink to derive Cartesian position  $x = (x, y, \phi)$ from encoders information L at real time. Moreover, this routine is used to find required internal forces from (7).

#### V. EXPERIMENTAL RESULTS

In order to show the effectiveness of the proposed control algorithm, several experiments are performed. In the first set of experiments, two disjointed linear motions in translation and rotation are considered. In these experiments, step input as a set point is applied to the robot. Step function has this feature that it can excite almost all dynamics of the system. As a result, investigation of the step response can be a suitable measure in performance evaluation of the robot. Furthermore, a more challenging circular profile is considered in the next experiment, to track a circular path of 0.2m about the central position. For the first experiment, suppose that

<sup>1</sup>C code for Feasible Sequential Quadratic Programming



Fig. 7. Cascade control block diagram



Fig. 8. Implementation results showing the actual and desired position and orientation of the end-effector for  $\boldsymbol{x}_d = [0, 0.25, 0]^T$ 



Fig. 9. Implementation results showing the cables tension for  $\boldsymbol{x}_d = [0, 0.25, 0]^T$ 



Fig. 10. Implementation results showing the actual and desired position and orientation of the end-effector for  $\boldsymbol{x}_d = [0, 0, \pi/6]^T$ 



Fig. 11. Implementation results showing the cables tension for  $\boldsymbol{x}_d = [0, 0, \pi/6]^T$ 

the initial position of the end-effector is  $\boldsymbol{x} = [0, 0, 0]^T$  in SI units and the desired end-effector position and orientation is  $\boldsymbol{x}_d = [0, 0.25, 0]^T$ . The results of implementation using proposed PID control (4) in companion with the internal force control structure, are given in Fig. (8). As it is seen in this figure, position and orientation outputs suitably track the desired trajectories and the steady state errors are very small, while as it is shown in Fig. (9) all cables remain in tension for the whole maneuver. The prescribed uniformly ultimately

bounded tracking error for the control structure is verified in all three directions in this experiment.

In the next experiment, suppose that the desired orientation of the end-effector is  $x_d = [0, 0, \pi/6 \, rad]^T$ , while the same controller gains are considered. The results of this experiment are given in Fig. (10). As it is observed, tracking performance is very suitable and the position errors in x and y directions are small and in order of  $10^{-3}$ . Furthermore, as it is shown in Fig. (11), all cables are in tension.



Fig. 12. Implementation results showing circular trajectory generation by the end-effector



Fig. 13. Implementation results showing the rotation  $\phi$  during circular trajectory generation

For the circular profile, the end-effector is commanded to track a circle with radius of 0.2 meter in 10 seconds, while attempting to maintain zero orientation  $\phi = 0$ , at all times. The reference Cartesian positions for this experiment are  $x = 0.2 \cos(0.2\pi t)$  and  $y = 0.2 \sin(0.2\pi t)$ . Figures (12) and (13) show the reference and actual circle and deviation of  $\phi$  from its zero desired value. It is shown that the simple PID control scheme is capable to stabilize the system and performs such maneuver, while the absolute positioning errors are relatively small. As it is seen in Fig. (13), orientation error in this test is very small and in order of  $10^{-3}$ 

#### VI. CONCLUSIONS

This paper addresses the issues of dynamic analysis and control of a planar cable-driven robot in an experimental prospective. To develop the idea, kinematics and dynamics of the planar cable-driven robot are firstly studied. According to unique property of the cables that can only apply tensile forces, and in order to ensure that all the cables are in tension at all times, internal force control structure is used with proposed PID algorithm. A robust PID controller is proposed to overcome partial knowledge of the robot, and to keep the tracking errors bounded. Next, important aspects in implementation of the robot are discussed and control structure of the robot is proposed using cascade control concept. Finally, several experiments on K.N. Toosi planar cable-driven robot are performed. The results show suitable tracking capability of the robot with different desired trajectories, while all the cables remain in tension at all times.

#### REFERENCES

- M.A. Khosravi and H.D. Taghirad, *Dynamic Analysis and Control of Cable Driven Robots with Elastic Cables*. Trans. Can. Soc. Mech. Eng., Vol. 35, No. 4, pp. 543-557, 2011.
- [2] R. Bostelman, J. Albus, N. Dagalakis, and A. Jacoff, *Applications of the NIST Robocrane*. Proceedings of the 5<sup>th</sup> International Symposium on Robotics and Manufacturing, 1994, pp. 403-410.
- [3] S. Kawamura, H. Kino, and C. Won, *High-speed manipulation by using parallel wire-driven robots*. Robotica, Vol. 18, No. 3, pp. 13-21, 2000.
- [4] K. Maeda, S. Tadokoro, T. Takamori, M. Hiller, and R. Verhoeven, On design of a redundant wire-driven parallel robot WARP manipulator. Proceedings of IEEE International Conference on Robotics and Automation, 1999, pp. 895-900.
- [5] R. Roberts, T. Graham, and T. Lippitt, On the Inverse Kinematics, Statics, and Fault Tolerance of Cable-Suspended Robots. Journal of Robotic Systems, Vol. 15, No. 10, pp. 649-661, 1998.
- [6] L. Cone, Skycam: An aerial robotic camera system. Byte, vol. 10, pp. 122132, 1985.
- [7] H.D. Taghirad and M. Nahon, *Kinematic Analysis of A Macro–Micro Redundantly Actuated Parallel Manipulator*. Advanced Robotics, Vol. 22, No. 6-7, pp. 657-87, 2008.
- [8] A. Riechel, P. Bosscher, H. Lipkin, and I. Ebert-Uphoff, *Concept paper: Cable-driven robots for use in hazardous environments*. Proceedings of 10th Int. Topical Meet. Robot Remote Syst. Hazardous Environ., Gainesville, 2004, pp. 310-317.
- [9] A. Alp and S. Agrawal, *Cable Suspended Robots: Feedback Controllers with Positive Inputs.* Proceedings of the American Control Conference, 2002, pp. 815-820.
- [10] R.L. Williams, P. Gallina, and J. Vadia, *Planar Translational Cable Direct Driven Robots.*, Journal of Robotic Systems, Vol. 20, No. 3, pp. 107-120, 2003.
- [11] S.R. Oh and S. Agrawal, Cable Suspended Planar Robots with Redundant Cables: Controllers with Positive Tensions., IEEE Trans. on Robotics, Vol. 21, No. 3, pp. 457-465, 2005.
- [12] Y. Babazedeh, H.D. Taghirad, and M.M. Aref, *Dynamics analysis of a redundant parallel manipulator driven by elastic cables.* Proceedings of the IEEE 10th International Conference on Control, Automation, Robotics and Vision, 2008, pp. 536-542.
- [13] M.A. Khosravi and H.D. Taghirad, Robust PID Control of Fully-Constrained Cable Driven Parallel Robots. submitted to Mechatronics, 2012.
- [14] Plasma Cables, http://www.cortlandcompany.com, 2012.
- [15] RT-LAB version 8 User Guide., Opal-RT Company, 2005.
- [16] C. Lawrence, J.L. Zhou, and A.L. Tits, User's Guide for CFSQP Version 2.0: A C Code for Solving Constrained Nonlinear Optimization Problems, Generating Iterates Satisfying All Inequality Constraints., Technical Report, Institute for systems Research, University of Maryland, TR-94-16, 1994.